

Faculty of Computer Science Institute of Systems Architecture, Privacy and Data Security Research Group

Linear Row and Column Predictors for the Analysis of Resized Images

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Resampling Detection

- resizing/scaling is a common digital image processing primitive
- ▷ pre- or post-processing; or part of more complex manipulations



Resampling Detection

- resizing/scaling is a common digital image processing primitive
- ▷ pre- or post-processing; or part of more complex manipulations
- resampling to a new image grid; involves an interpolation step
- interpolation introduces periodic linear correlations between neighboring pixels



 analysis and detection of interpolation artifacts is of interest in forensic settings, but also in steganalysis or digital watermarking Interpolation of 1D Signals

$$s(x) = \sum_{\chi = -\infty}^{\infty} h(x - \chi) s(\chi) \quad (x \in \mathbb{R}, \chi \in \mathbb{Z})$$

• interpolation weights $h(x - \chi)$ depend on the relative position $\delta_x = x - \lfloor x \rfloor$, which is a periodic function: $\delta_x = \delta_{x+1}$

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Interpolation of 1D Signals



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$$\triangleright \ \omega = \frac{q}{p} \text{ with } p \perp q \implies \delta_{\omega\chi'} = \delta_{\omega(\chi'+p)}$$

 \triangleright interpolation weights are periodic with p

Interpolation of 1D Signals



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state-of-the-art resampling detection relies on linear predictor residue

[Popescu & Farid, TSP 2005], [Kirchner, MMSec 2008]



samples are modeled as linear combination of their neighbors

$$e_i = s'_i - \sum_{\substack{|k| \le K \\ k \neq 0}} \alpha_k \, s'_{i+k}$$

► large absolute prediction errors indicate minor degree of linear dependence

• interpolation causes periodic artifacts in the residue signal e_i

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[Popescu & Farid, TSP 2005], [Kirchner, MMSec 2008]

fixed predictor coefficients throughout the whole signal

(EM estimate or pre-set)

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slide 3 of 11

Fixed predictor coefficients α are not ideal to **model** interpolated signals



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A Refined Model

Fixed predictor coefficients α are not ideal to **model** interpolated signals

 \blacktriangleright phase-dependent coefficients $\pmb{\alpha}^{(i)}$ would better reflect the actual correlation for a specific sample s'_i

$$s_i' = \sum_{\substack{|k| \leq K \\ k \neq 0}} \alpha_k^{(i)} \, s_{i+k}' + e_i$$

• scaling/resizing with scaling factor $\omega^{-1} = p/q$: $\alpha^{(i)} = \alpha^{(i+lp)}$

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- ▶ scaling/resizing with scaling factor $\omega^{-1} = p/q$: $\alpha^{(i)} = \alpha^{(i+lp)}$
- upsampling: $\forall i \exists \alpha^{(i)} e_i = 0$ (for suitable neighborhood sizes K)
- downsampling: model error depends on interpolation kernel and scaling factor (never vanishes for linear interpolation kernel)

A Refined Model

- Fixed predictor coefficients α are not ideal to **model** interpolated signals
- phase-dependent coefficients α⁽ⁱ⁾ would better reflect the actual correlation for a specific sample s'_i

$$s_i' - \eta_i' = \sum_{\substack{|k| \leq K \\ k \neq 0}} \alpha_k^{(i)} \left(s_{i+k}' - \eta_{i+k}' \right) + e_i$$

quantization/rounding noise

► scaling/resizing with scaling factor $\omega^{-1} = p/q$: $\alpha^{(i)} = \alpha^{(i+lp)}$

• upsampling: $\forall i \exists \alpha^{(i)} e_i = 0$ (for suitable neighborhood sizes K)

- downsampling: model error depends on interpolation kernel and scaling factor (never vanishes for linear interpolation kernel)
- explicit model for linear correlations in scaled/resized signals
- \triangleright estimation of coefficients $oldsymbol{lpha}^{(i)}$?

Resizing of Digital Images

assumption: separable interpolation kernel

▷ effects of resizing can be analyzed for each row / column independently

 $r^{(i-3)}$ $r^{(i-2)}$ $r^{(i-1)}$ $r^{(i)}$ $r^{(i+1)}$ $r^{(i+2)}$ $r^{(i+3)}$

Resizing of Digital Images

assumption: separable interpolation kernel

- ▷ effects of resizing can be analyzed for each row/column independently
- ▷ all pixels within one row/column are equally correlated with their vertical/horizontal neighbors



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 linear regression model to estimate 'tailored' predictior coefficients

$$\begin{split} \boldsymbol{r}^{(i)} - \boldsymbol{\eta}^{(i)} &= \sum_{\substack{|k| \leq K \\ k \neq 0}} \boldsymbol{\alpha}_{k}^{(i)} \left(\boldsymbol{r}^{(i-k)} - \boldsymbol{\eta}^{(i-k)} \right) + \boldsymbol{e}^{(i)} \\ &= \left(\mathbf{R}^{(i)} - \mathbf{N}^{(i)} \right) \cdot \boldsymbol{\alpha}^{(i)} + \boldsymbol{e}^{(i)} \end{split}$$

one regression per row/column

• ideal case: vanishing model error $e^{(i)}$

(e.g. for upsampling)

$$\boldsymbol{r}^{(i)} - \boldsymbol{\eta}^{(i)} = \left(\mathbf{R}^{(i)} - \mathbf{N}^{(i)} \right) \cdot \boldsymbol{\alpha}^{(i)}$$

- $\mathbf{r}^{(i)} \mathbf{\eta}^{(i)} = \left(\mathbf{R}^{(i)} \mathbf{N}^{(i)} \right) \cdot \mathbf{\alpha}^{(i)}$ (e.g. for upsampling) $\mathbf{r}^{(i)} - \mathbf{\eta}^{(i)} = \left(\mathbf{R}^{(i)} - \mathbf{N}^{(i)} \right) \cdot \mathbf{\alpha}^{(i)}$ measurement errors on both sides
- hinspace total least squares (TLS) estimate $\hat{oldsymbol{lpha}}^{(i)}$

 $\hat{\boldsymbol{r}}^{(i)} = \hat{\boldsymbol{R}}^{(i)} \cdot \hat{\boldsymbol{\alpha}}^{(i)} \quad \text{such that } \left\| \begin{bmatrix} \boldsymbol{R}^{(i)}, \boldsymbol{r}^{(i)} \end{bmatrix} - \begin{bmatrix} \hat{\boldsymbol{R}}^{(i)}, \hat{\boldsymbol{r}}^{(i)} \end{bmatrix} \right\|_{F} \rightarrow \min$

► ideal case: vanishing model error $e^{(i)}$ (e.g. for upsampling) $r^{(i)} - \tilde{\eta}^{(i)} = \left(\mathbf{R}^{(i)} - \mathbf{N}^{(i)}\right) \cdot \boldsymbol{\alpha}^{(i)}$ measurement errors on both sides ▷ total least squares (TLS) estimate $\hat{\boldsymbol{\alpha}}^{(i)}$

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example: estimates for 150 % bilinear upsampling ($\omega = 2/3, K = 3$)



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 periodic artifacts in predictor coefficients can be exploited for detection of resizing

(e.g. for upsampling)

 'direct' analysis instead of implicit measurement via the predictor residue

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- hinspace total least squares (TLS) estimate $\hat{oldsymbol{lpha}}^{(i)}$
- ideal world hardly ever matches reality; model error is negligible only if
 - > interpolation parameters permit a complete model
 - neighborhood size is chosen correctly

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large model error violates homoscedasticy assumption

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- TLS estimates may become instable
- **but:** resampling detection does not require *exact* knowledge of α



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bias towards left and right neighbors gradually varies



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simplified predictor model:

 $\boldsymbol{r}^{(i)} = \mathbf{R}^{(i)} \cdot \boldsymbol{\beta}^{(i)} + \boldsymbol{\varepsilon}^{(i)}$

bias towards left and right neighbors gradually varies



► simplified predictor model: $\mathbf{r}^{(i)} = \mathbf{R}^{(i)} \cdot \boldsymbol{\beta}^{(i)} + \boldsymbol{\varepsilon}^{(i)}$ ▷ weighted least squares (WLS) estimate $\hat{\boldsymbol{\beta}}^{(i)}$

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- ► simplified predictor model: $\mathbf{r}^{(i)} = \mathbf{R}^{(i)} \cdot \boldsymbol{\beta}^{(i)} + \boldsymbol{\varepsilon}^{(i)}$ ▷ weighted least squares (WLS) estimate $\hat{\boldsymbol{\beta}}^{(i)}$
- one possible (very coarse) analysis:

$$d_i = \hat{\beta}_{-1}^{(i)} - \hat{\beta}_1^{(i)}$$

Spectral Analysis

- \blacktriangleright resizing causes periodic artifacts in the predictor coefficients, or their differences d_i
- typical detectors work in the frequency domain (Fourier spectrum)
- but: estimated coefficients are error-prone and hardly exhibit a perfectly periodic behavior
 - ▷ robust spectral density estimation

here: based on Spearman's rank correlation coefficient [Ahdesmäki et al., BMC Bioinf. 2005]

$$S_{\varrho}(f) = \sum_{l=-L}^{L} \varrho(l) \exp(-2\pi i f l)$$

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downsampling to 80 %, cubic spline interpolation, 512 imes 512 image

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Experimental Setup

- ► test database of ≈1100 never-compressed images (five different camera models) from the **Dresden Image Database** [Gloe & Böhme, ACM SAC 2010]
- resizing of the green channel with ImageMagick's convert
 four different interpolation kernels

	bilinear	bicubic	windowed sinc	cubic spline
-filter	Triangle	Catrom	Lanczos	Cubic

• analysis of the center 512 \times 512 region, neighborhood size K = 3



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Results for Downsampling

benchmark detector: Popescu & Farid's EM-based global predictor [Popescu & Farid, 2005] detection rate at 1% false acceptance rate (TP_{0.01}), area under the ROC curve (AUC)



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superior (or at least comparable) detection results for row/column model

Results for Downsampling

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ROC curves for downsampling to 80 %



row/column model has strengths for more sophisticated kernels

- characteristic structure of resized images suggests row/column predictors to analyze traces of interpolation
 - ▷ one linear regression per row/column
 - ▷ measure periodic artifacts in a series of predictor coefficients
- experiments show promising results compared to state-of-the-art

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no straight-forward extension to general geometric transformations

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 distinguish upsampled from downsampled images



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- incorporate image models





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Thanks for your attention

Questions?

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